# Atoms, X-rays and Synchrotron Radiation

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**INSPYRE** 2017 – INternational School on modern Physics and Research

13-17 February 2017 INFN - Frascati National Laboratory

## Outline

- Light
- X-rays and Synchrotron radiation sources

   X-rays and atoms
   X-ray sources
- Detectors Basic Principles
  - Interactions of x-rays with matter
  - XAFS: EXAFS and XANES
- Gas Detectors
  - Ionization chambers
- Conclusions



Light

Progress in science goes in parallel with the technical progress in producing and using light at different wavelengths to explore the physical world.



Visible light is only a tiny slice of the electromagnetic spectrum. The entire electromagnetic spectrum of light is huge, spanning from gamma rays on one end to radio waves.



*Physiologically we see these frequencies because the photoreceptors in our retinas are sensitive to them.* When photons of light hit the photoreceptors this creates an electrochemical signal which is the first step in a fascinating process which ultimately results in us seeing colors.

### Light and waves



#### Electromagnetic Spectrum



The wavelength ( $\lambda$ ) and frequency ( $\nu$ ) of light are strictly related: the higher the frequency the shorter the wavelength! This is because all light waves more through vacuum at the same speed (c = speed of light) and the equation that relates wavelength and frequency for electromagnetic waves is:  $\lambda \nu = c$ 



X-rays discovery



While Wilhelm Roentgen was working on the effects of cathode rays during 1895, he discovered X-rays. His experiments involved the passing of electric current through gases at extremely low pressure. On November 8, 1895 he observed that certain rays were emitted during the passing of the current through discharge tube. His experiment that involved working in a totally dark room with a well covered discharge tube resulted in the emission of rays which illuminated a barium platinocyanide screen. The screen became fluorescent even though it was placed two meters away from discharge tube.



Gas tube: electrons are freed from a cold cathode by positive ion bombardment, thus necessitating a certain gas pressure.

He continued his experiments using photographic plates and generated the very first "roentgenogram" by developing the image of his wife's hand and analyzed the variable transparency as showed by her bones, flesh and her wedding ring.



Wilhelm Conrad Roentgen



Electromagnetic Spectrum and X-rays





Matter is everything around us! All matter such as solids, liquids, and gases, is composed of atoms. Therefore, atoms are considered to be the basic building block of matter. From the periodic table, it can be seen that there are only about 100 different kinds of atoms. These same 100 atoms form thousands of different substances ranging from the air we breathe to the metal used to support tall buildings.

#### Atomic Solid The colspan="2">The colspan="2">Color Key Atomic Solid The colspan="2">Color Key

Alkali



elements. wlonk.com Copyright @ 2005 Keith Enevoldsen See website for terms of use

Noble

## Atoms and physical properties



Gold coins and ingots have been highly prized for millennia. But scientists have realized that nanoparticles of this metal could have also quite important properties. In labs around the world, gold nanoparticles are being tested as components in technology and medicines. Gold nanoparticles could be used to kill cancer cells, improve the efficiency of solar cells and catalyze chemical reactions.

X-rays and Atoms



Graphite is opaque and metallic- to earthy-looking, while diamonds are transparent and brilliant.

The different properties of graphite and diamond arise from their distinct crystal structures.

#### X-rays application fields



## Synchrotron radiation sources

Light sources

Fire is not a very useful light source to see small details because its emitted power is spread in all directions!





A torchlight is more adequate because due to its small size the emission is concentrated within a narrow angular spread: this a "bright" source!



Synchrotron radiation is a very bright light source that, as will be shown, gives us the chance to study also things that we cannot "see " with our eyes using not visible light but X-rays!



Light sources and brightness

When interested in nm scale details: brightness becomes fundamental.

A bright source is the one very effective in illuminating a specific target. If the specific target is small a bright source is a small size source with emission concentrated within a narrow angular spread.





Bright X-ray sources?

# HE particle accelerators

# Relativistic effects



#### Synchrotron light is present in nature!



Synchrotron radiation is a very important emission process in astrophysics!

Crab Nebula: remnant of a supernova explosion seen on earth by Chinese astronomers in 1054, at about 6500 light years from Earth in the constellation Taurus !

SR emission is produced by high energy electrons whirling around the magnetic fields lines originating from a Pulsar

NASA Hubble Space Telescope image of the Crab Nebula (NASA, ESA and Allison Loll/Jeff Hester (Arizona State University)).





NASA's Great Observatories' View of the Crab Nebula X-Rayblue: NASA/CXC/J.Hester (ASU); Optical-red and yellow: NASA/ESA/J.Hester & A.Loll (ASU); Infrared-purple: NASA/ JPL-Caltech/R.Gehrz (Univ. Minn.) The heart of the nebula is a rapidly-spinning neutron star, a pulsar, that powers the strongly polarised bluish 'synchrotron' nebula.

The Crab pulsar is slowing at the rate of about 10<sup>-8</sup> sec per day, and the corresponding energy loss agrees well with the energy needed to keep the nebula luminous. Some of this luminosity takes the form of synchrotron radiation, requiring a source of energy for accelerating charged particles.

Composite image data from three of NASA's Great Observatories. The Chandra X-ray Observatory image is shown in blue, the Hubble Space Telescope optical image is in red and yellow, and the Spitzer Space Telescope's infrared image is in purple. The X-ray image is smaller than the others because extremely energetic electrons emitting X-rays radiate away their energy more quickly than the lower-energy electrons emitting optical and infrared light. The Crab Nebula is one of the most studied objects in the sky, truly making it a cosmic icon.

Synchrotron radiation

Accelerated NON relativistic charged particle, e<sup>+</sup>, e<sup>-</sup> and ions, emit electromagnetic radiation like electric charges forced to oscillate along an antenna.

 $v \ll c \text{ or } \beta = v/c \ll 1$ 



 $v \approx c \text{ or } \beta = v/c \approx 1$ 

When charged particles, moving at RELATIVISTIC speeds (v ≈ c), are forced to change the direction of their motion (acceleration), under the effect of magnetic fields, in circular particle accelerators, like synchrotrons, the radiation produced is called Synchrotron Radiation.



# Synchrotron light is artificially produced by relativistic particles accelerated in circular orbits.



... and synchrotron radiation is also the coherent radiation emitted by the undulators of Free Electron Lasers.

# Radiation sources





Bending magnet

Undulator



There are two different sources of radiation in a storage ring:

- bending magnets (BMs)
- insertion devices (IDs) or periodic arrays of magnets inserted between the BMs (wigglers and undulators)



 $DA\Phi NE$  bending magnet (BM)



ESRF Insertion Device (ID) - Undulator

BM and ID have different characteristics concerning, spectral distribution, flux, brightness and polarization.



## Synchrotron radiation: history



1947 General Electric Res. Lab. - 70 MeV Electron Synchrotron - N.Y. USA

#### Starting point: Proof of concepts, tests of theories!

- In the 50s and 60s machines built for High Energy Physics: synchrotrons (*1947 First 'visual observation of synchrotron radiation*).
- Synchrotron radiation was considered a nuisance by particle physicists: unwanted but unavoidable loss of energy!
- 1961 US National Bureau of Standards (now NIST) modified their electron synchrotron : access to the synchrotron radiation users.
- Synchrotron radiation scientists became parasites of nuclear physics experiments. (1961 Frascati – CNEN Electrosynchrotron – (0.4–1.1) GeV)
- 1968 *First storage ring dedicated* to synchrotron radiation research: *Tantalus* (University of Wisconsin) only *bending magnets*.

F.R. Elder, A.M. Gurewitsch, R.V. Langmuir, and H.C. Pollock, Radiation from Electrons in a Synchrotron, Phys. Rev. 71,829 (1947) G. C. Baldwin and D.W. Kerst, Origin of Synchrotron Radiation, Physics Today, 28,9 (1975)

Synchrotrons and Storage Rings



E= particle energy >>  $m_0c^2$   $E_{CM}=$  center-of-mass energy

## Synchrotron radiation: short history

#### Frascati: ElettroSynchrotron, ADA and ADONE

Frascati - CNEN (Comitato Nazionale Energia Nucleare) Laboratory ElettroSincrotrone - (0.4-1.1) GeV, C= 28 m (1959-1975)

![](_page_25_Picture_3.jpeg)

![](_page_25_Picture_4.jpeg)

LNF ADA (Anello Di Accumulazione) - first electron-positron storage ring (proposed by B. Touschek) 0.25 GeV, C= 5 m (1961-1964)

LNF ADONE (big ADA) electron-positron storage ring 1.5 GeV per beam, C = 105 m (1969-1993)

1976-1993 LNF ADONE 1.5 GeV parasitic/dedicated use for SR experiments after its use for HE experiments.

![](_page_25_Picture_8.jpeg)

#### Schematic view of a Synchrotron Radiation facility

![](_page_26_Picture_1.jpeg)

As a function of the energy range to be used each beamline must be optimized for a particular field of research.

Beamline schematic composition:

Front end

•

- Optical hutch
- Experimental hutch
- Control and computing

The *front end* isolates the beamline vacuum from the storage ring vacuum; defines the angular acceptance of the synchrotron radiation via an aperture; blocks(beam shutter) when required, the x-ray and Bremsstrahlung radiation during access to the other hutches.

# Synchrotron radiation properties

### Synchrotron radiation: physics

#### Relativistic focusing of Synchrotron Radiation

![](_page_28_Figure_2.jpeg)

 $v \approx c \text{ or } \beta = v/c \approx 1$ 

For a *relativistic effect*, when the speed of the emitting electrons increases to relativistic values (v ≈ c) the radiation pattern is compressed into a *narrow cone in the direction of motion, resulting into an emission tangential to the particle orbit.* 

Radiated power:

![](_page_28_Figure_6.jpeg)

Q = particle charge, E = particle energy, m<sub>o</sub> = rest mass, R = radius of curvature

1949 Schwinger: classical theory of radiation from accelerated relativistic electrons

![](_page_29_Picture_0.jpeg)

ASTRID (Aarhus - Denmark) http://www.isa.au.dk/animations/pictures/pic-index.asp

http://www.isa.au.dk/animations/Finalmovie/astrid\_total\_v2.mov

#### Synchrotron Radiation Properties

What makes synchrotron radiation interesting, powerful and unique?

- Continuum source from IR to X-rays (tunability) which covers from microwaves to hard X-rays: the user can select the wavelength required for experimentcontinuous (Bending Magnet/Wiggler) - quasimonochromatic (Undulator)
- Source in a clean UHV environment
- Very high flux and brightness (with undulators) highly collimated photon beams generated by a small divergence and small size sources .
- Highly Polarized
- *Pulsed time structure* pulsed length down to tens of picoseconds allows the resolution of processes on the same time scale
- High stability (submicron source stability)

![](_page_30_Figure_8.jpeg)

#### Spectral range covered by Synchrotron Radiation!

#### THE ELECTROMAGNETIC SPECTR

![](_page_31_Figure_2.jpeg)

![](_page_32_Picture_0.jpeg)

![](_page_33_Picture_0.jpeg)

Synchrotron radiation sources have very high brightness.

![](_page_33_Figure_2.jpeg)

Spectral brightness is that portion of the brightness lying within a *relative* spectral bandwidth  $\Delta\omega/\omega$ :

Spectral Brightness= second  $\cdot$  mrad<sup>2</sup>  $\cdot$  mm<sup>2</sup>  $\cdot$  0.1%BW

photons

![](_page_33_Picture_5.jpeg)

#### **3rd Generation Light Sources**

![](_page_34_Picture_1.jpeg)

![](_page_34_Picture_2.jpeg)

![](_page_34_Picture_3.jpeg)

ESRF - France

DIAMOND - UK

ALBA - Spain

Brightness is the main figure of merit of synchrotron radiation sources and its huge increase, was obtained designing low emittance machines, minimizing the source size and the beam divergence.

#### Ultimate SR facilities

![](_page_34_Picture_9.jpeg)

Lund - Sweden

Sirius - Brazil

Shanghai -China

#### Synchrotron radiation @ INFN-Frascati National Laboratory

![](_page_35_Picture_1.jpeg)




#### **INFN-LNF** Synchrotron Radiation Facility





## Available techniques

- FTIR spectroscopy, IR microscopy and IR imaging
- UV-Vis absorption spectroscopy
- Photochemistry: UV irradiation and FTIR microspectroscopy and imaging.
- Soft x-ray spectroscopy: XANES (X-ray Absorption Near Edge Structure) light elements from Na to S
- SEY (secondary electron yield) and XPS (X-ray photoelectron spectroscopy) - by electron and photon bombardment

# From accelerators to applications



E. Malamud Ed., Accelerators and Beams tools of discovery and innovation (http://www.aps.org/units/dpb/news/edition4th.cfm) 2013

# Interactions of x-rays with matter

**Photoelectric effect** 

Electromagnetic radiation can be used to push electrons, freeing them from the surface of a solid. This process is called the *photoelectric effect* (or *photoelectric emission*), a material that can exhibit this phenomena is said to be *photoemissive*, and the ejected electrons are called *photoelectrons*; but there is nothing that would distinguish them from other electrons. All electrons are identical to one another in mass, charge, spin, and magnetic moment.



The photoelectric effect does not occur when the frequency of the incident light is less than the threshold frequency. Different materials have different threshold frequencies.

# Photoelectric effect

Classical physics cannot explain why...

no photoelectrons are emitted when the incident light has a frequency below the threshold,
the maximum kinetic energy of the photoelectrons increases with the frequency of the incident light,

- the maximum kinetic energy of the photoelectrons is independent of the intensity of the incident light, and

- there is essentially no delay between absorption of the radiant energy and the emission of photoelectrons.

Modern physics states that...

- electromagnetic radiation is composed of discrete entities called photons

- the energy of a photon is proportional to its frequency

- the work function of a material is the energy needed per photon to extract an electron from its surface



In 1905, *Albert Einstein realized that light was behaving as if it was composed of tiny particles* (initially called quanta and later called photons) and that the energy of each particle was proportional to the frequency of the electromagnetic radiation (Nobel Prize in Physics in 1921).

## Interaction of X-rays with matter

#### Attenuation mechanisms for X-rays





Fluorescence XRF & Imaging, XAFS

## Some X-ray techniques



# X-ray Absorption Spectroscopy

XAS local sensitive and chemical selective probe that can provide structural, electronic and magnetic information.



# DAFNE-L DXR1 beam line absorption spectroscopy



 $I_0$ ,  $I_1$ ,  $I_2$  Gas ionization chambers -  $I_F$  SDD solid state detector



### DAPNE Soft X-ray DXR1 Beamline

- Wiggler soft x-ray beam line
- Critical energy  $E_c = 284 \text{ eV}$
- Working range 0.9 3.0 keV
- TOYAMA double crystal monochromator with KTP (011), Ge (111), Si (111), InSb (111) and Beryl (10-10) crystals
- Soft X-ray absorption spectroscopy and tests of Soft x-ray optics and detectors.

# DXR1 Beamline

As a function of the energy range to be used each beamline must be optimized for a particular field of research. The front end isolates the beamline vacuum from the storage ring vacuum; defines the angular acceptance of the synchrotron radiation via an aperture; blocks (beam shutter) when required, the x-ray and Bremsstrahlung radiation during access to the other hutches.





Monochromator



# Monochromator



Prism and visible light



#### X-rays and crystals



Crystal type	2d spacing (Å)	Energy range (eV)	Absorption edges				
Beryl (10-10)	15.954	1000 - 1560	Na K, Mg K, Cu L				
KTP (011)	10.950	1200 - 2200	Mg K, Al K				
InSb (111)	7.481	1800 - 3100	Si K, P K, S K, Cl K				
Ge (111)	6.532	2100 - 3100	P K, S K, Cl K				







Detectors and experimental chamber

## Elements that can be investigated

1 H					С	K- ea	lges									1 H	2 He
1.00794						_										1.00794	4.002602
3 Li 6.941	4 Be 9.012182					L - ed	ges	1				5 B 10.811	6 C 12.0107	7 N 14.00674	8 O 15.9994	9 F 18.998403:	10 Ne 20.1797
11 Na 22.989770	12 Mg 24.3050				1	И - ес	dges					13 Al 26.981538	14 Si 28.0855	15 P 30.973761	16 S 32.066	17 Cl 35.4527	18 Ar 39.948
19 K 39.0983	20 Ca 40.078	21 Sc 44.955910	22 Ti 47.867	23 V 50.9415	24 Cr 51.9961	25 Mn 54.938049	26 Fe 55.845	27 CO 58.933200	28 Ni 58.6934	29 Cu 63.546	30 Zn 65.39	31 Ga 69.723	32 Ge 72.61	33 As 74.92160	34 Se 78.96	35 Br 79.904	36 Kr 83.80
37 Rb 85.4678	38 Sr 87.62	39 Y 88.90585	40 Zr 91.224	41 Nb 92.90638	42 Mo 95.94	43 Tc (98)	44 Ru 101.07	45 Rh 102.90550	46 Pd 106.42	47 Ag 107.8682	48 Cd 112.411	49 In 114.818	50 Sn 118.710	51 Sb 121.760	52 Te 127.60	53 I 126.90447	54 Xe 131.29
55 CS 132.90545	30 Ba 137.327	57 La 138.9055	72 Hf 178.49	73 Ta 180 9479	/4 W 183.84	75 Re 186.207	76 Os 190.23	Ir 192 217	78 Pt 195.078	79 Au 196.96655	80 Hg 200.59	81 Tl 204.383	82 Pb 207.2	83 Bi 208.98038	84 Po (209)	85 At (210)	86 Rn (222)
87 Fr (223)	88 Ra (226)	89 Ac (227)	104 Rf (261)	105 Db (262)	106 Sg (263)	107 Bh (262)	108 Hs (265)	109 Mt (266)	110 (269)	111 (272)	112 (277)		114 (289) (287)		116 (289)		(293)

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
140.116	140.90765	144.24	(145)	150.36	151.964	157.25	158.92534	162.50	164.93032	167.26	168.93421	173.04	174.967
90	91	92	93	94	95	96	97	98	99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk (247)	Cf	Es	Fm	Md	No	Lr
232.0381	231.03588	238.0289	(237)	(244)	(243)	(247)		(251)	(252)	(257)	(258)	(259)	(262)







# Photons as Ionizing Radiation

- Photoelectric effect
  - Causes ejection of an inner orbital electron and thus also characteristic radiation (energy of fluorescence lines  $E_F \approx Z^2$ ) as orbital hole is filled
  - Energy of ejected photoelectron:  $E_e = hv - E_B$







## **Photoelectric** absorption

The probability of a photoelectric interaction is a function of the photon energy and the atomic number of the target atom.

A photoelectric interaction cannot occur unless the incident x-ray has energy equal to or greater than the electron binding energy.



Absorption and decay effects XRF (X Ray Fluorescence) and AES (Auger Electron).



XAFS = XANES + EXAFS



# XANES and Carbon K edge





#### Extended X ray Absorption Fine Structure

#### **EXAFS** phenomenological interpretation



Auto -interference phenomenon of the outgoing photoelectron with its parts that are backscattered by the neighbouring atoms

X-ray Absorption



E. Borfecchia et al. - DOI: 10.1098/rsta.2012.0132



**EXAFS** 



## **EXAFS and structural information**



EXAFS data analysis



# Cu foil and temperature effects







# EXAFS data analysis






### X ray Absorption Near Edge Structure





The local symmetry around the absorbing atom (symmetry, distance ligandmetal), the electronic structure of the absorbing atom (electronic filling of the valence state, oxidation state, spin state...)

Pre-edge region



Pre-edge peaks are due to electronic transitions (mainly dipole allowed) to empty bound states near the Fermi level.

states

level

The peak due to s --> p transitions ( K edge) provides information on the absorber local geometry. In the Tetrahedral case ( not centrosymmetric like Oh case) the p d mixing is allowed and this gives the largest pre-edge peak.

### Shape of whitelines and L-edges

Whitelines present in the L-edges of atoms with 4d and 5d electrons, reflect holes in d-bands: the intensity decreases as a function of the increasing number of electrons in the d-band. In Au the 5d band is full. Phys. Rev. B 36 (1987) 2972





### XANES and oxidation state





The edge,  $E_0$  (arrow), defines the onset of continuous states (this is not not the Fermi level).  $E_0$  is a function of the absorber oxidation state and geometry. It may also increase by several eV due to oxidation.

### Detectors and Gas ionization chambers

# X-ray Ion Chamber



Inside the detector, an electric field is applied across two parallel plates. Some of the x-rays in the beam interact with the chamber gas to produce fast photoelectrons, Auger electrons, and/or fluorescence photons. The energetic electrons produce additional electron-ion pairs by inelastic collisions, and the photons either escape or are photo-electrically absorbed. The electrons and ions are collected at the plates, and the current is measured with a low-noise current amplifier. The efficiency of the detector can be calculated from the active length of the chamber, the properties of the gas, and the x-ray absorption cross section at the appropriate photon energy.

## X-ray Ion chamber



#### Ion chamber with parallel plates.

#### Guard ring

In the parallel plate chamber the charge-collecting electrode is surrounded by an annular ring. The annular ring represents the guard ring (or guard electrode) and is separated from the collecting electrode by a narrow insulating gap, and the applied voltage to the guard ring is the same as that to the collecting electrode.

### Direct detection: charge conversion scheme and intensity measurement



The measured intensity is usually integrated during a well defined time interval and is proportional to the number of incident X-ray photons  $(N_{ph})$ .

Intrinsic statistical noise (Poisson statistics): 
$$\sigma_{N_{ph}} = \sqrt{N_{ph}} \quad \text{Effective:} \quad \sigma_{N_{ph}} = \sqrt{FN_{ph}}$$

Fano factor F accounts empirically for deviation from Poisson statistics  $F \approx 0.2$  for gasses,  $\approx 0.1$  for semiconductors



### Setup: XAFS in transmission mode

$$\mu(E) = \frac{1}{x} ln \left( \frac{I_0}{I_1} \right)$$

Current proportional to the x-ray intensity

Current amplifier and converter of I to V



H. Abe - A Brief Introduction to XAFS - SESAME JSPS School - 2011

Voltage to frequency converter and counter

# Ion chamber characteristics



Once the efficiency is known, the photon flux can be estimated from chamber current and the average energy required to produce an electron-ion pair

Efficiency of a 10-cm-long gas ionization chamber as a function of energy, for different gases at normal pressure. The efficiency of the detector can be calculated from the active length of the chamber, the properties of the chamber gas, and the x-ray absorption cross section at the appropriate photon energy

Element	Energy (eV)	
Helium	41	
Nitrogen	36	
Air	34.4	
Neon	36.3	
Argon	26	
Krypton	24	
Xenon	22	

## Photon flux evaluation

$$I = Ne = I_0 T\gamma e$$

*I*<sub>0</sub> = *Incoming photon flux (ph/s)* 

T = Ion chamber window transmission

γ = gas efficiency (electrons/ph)

 $\mu(cm^{-1}) = \left|\frac{\mu}{c}(E)\right| \rho$ 

L = length of the ion chamber plate

$$N \cong \frac{E}{\left\langle V_i \right\rangle}$$

N = Number of electron-ion pairs produced

E = X ray energy

 $\langle V_i \rangle$  = Average energy required to produce an electron-ion pair

$$I_{0}(ph/s) = \frac{I(A)}{\gamma e(C)} \frac{\langle V_{i} \rangle (eV)}{E(eV)} \frac{1}{1 - e^{-\mu L(cm)}}$$

- $\left\lfloor \frac{\mu}{\rho} \right\rfloor$  = gas mass attenuation coefficient
- ho = gas density function of pressure ( $\gamma$ )

 $\gamma = I_0 \ 10\%; \ I_1 \ 90\%$ 



X-ray ion chambers ad windows





Unmounted and mounted MOXTEK ultrathin windows







# Thank you for your attention



# Supplementary material



•	Speed of light		c = 2.99792458 × 10 <sup>8</sup> m/s
•	Electron charge		e = 1.6021 x10 <sup>-19</sup> Coulombs
•	Electron volts		1 eV = 1.6021x10 <sup>-19</sup> Joule
•	Energy and rest mass		1eV/c² = 1.78×10 <sup>-36</sup> kg
		Electron Proton	m <sub>0</sub> = 511.0 keV/c² = 9.109x10 <sup>-31</sup> kg m <sub>0</sub> = 938.3 MeV/c²= 1.673x10 <sup>-27</sup> kg
•	Relativistic energy, E		$E = mc^2 = m_0 \gamma c^2$
•	Lorentz factor, γ		γ =1/[(1-v²/c²) <sup>1/2</sup> ] = 1/ [(1-β²) <sup>1/2</sup> ] β= v/c
•	Relativistic momentum, p		$p = mv = m_{o\gamma}\beta c$
•	E-p relationship for ultra-relativistic	particles	$E^{2}/c^{2} = p^{2}+m_{0}c^{2}$ $\beta \approx 1, E=pc$
•	Kinetic energy		$T = E - m_0 c^2 = m_0 c^2 (\gamma - 1)$

## Anti-matter positron production



M. Calvetti, Antiparticelle accelerate, Asimmetrie 7, 16-21 (2008)